#### Mauro Anselmino: The transverse spin structure of the nucleon - III

#### About SSA in hadronic interactions

TMDs and SSA in inclusive hadronic interactions

TMDs and SSA in Drell-Yan processes

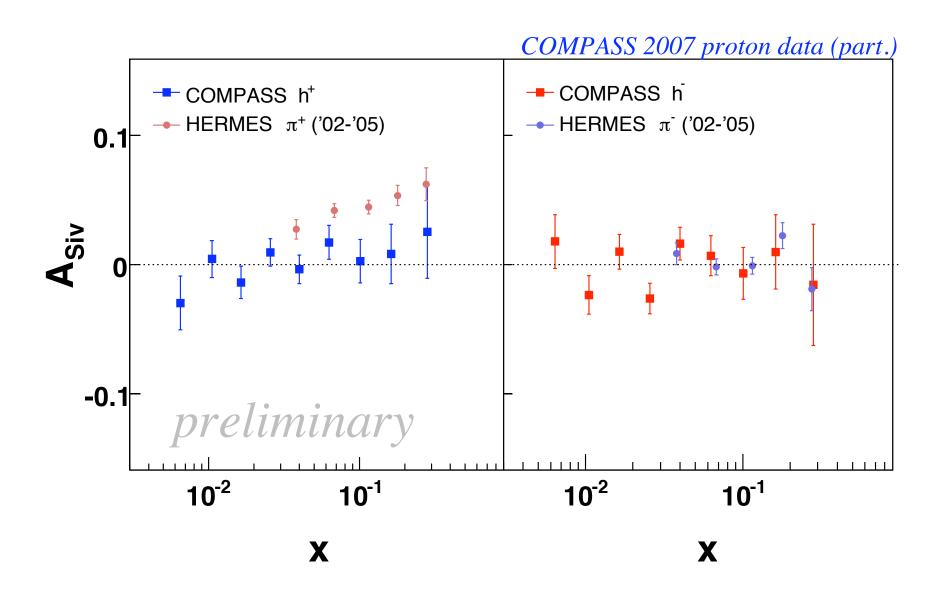
A fundamental QCD test

Drell-Yan processes, the transversity golden channel

Alternative ways to transversity

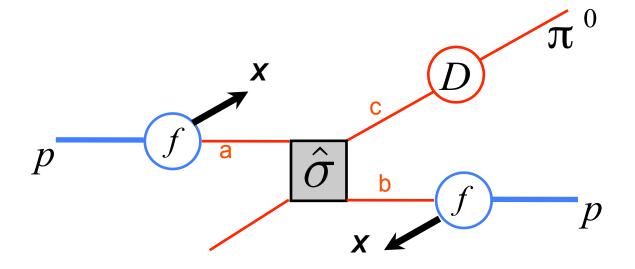
#### Sivers asymmetry: COMPASS vs HERMES

(F. Bradamante talk at Beijing workshop 2008)

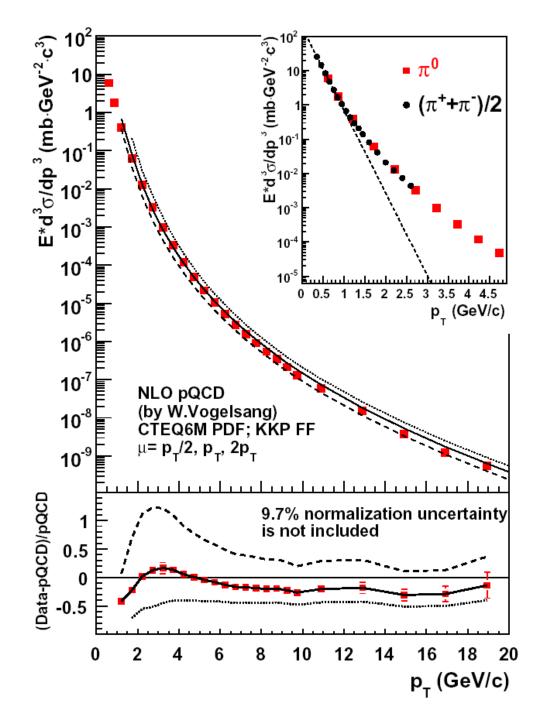


#### TMDs and SSAs in hadronic collisions

 $p\, p o \pi^0\, X$  (collinear configurations) factorization theorem



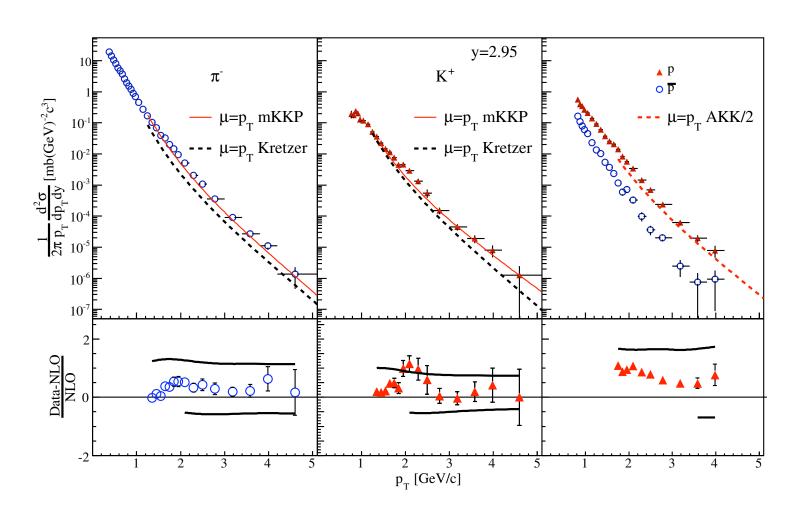
$$\mathrm{d}\sigma = \sum_{a,b,c,d=q,\bar{q},g} \underbrace{f_{a/p}(x_a) \otimes f_{b/p}(x_b)}_{\mathrm{PDF}} \otimes \mathrm{d}\hat{\sigma}^{ab \to cd} \otimes \underbrace{D_{\pi/c}(z)}_{\mathrm{FF}}$$
pQCD elementary interactions



RHIC, 
$$p p \rightarrow \pi X$$
  
 $\sqrt{s} = 200 \,\text{GeV}$ 

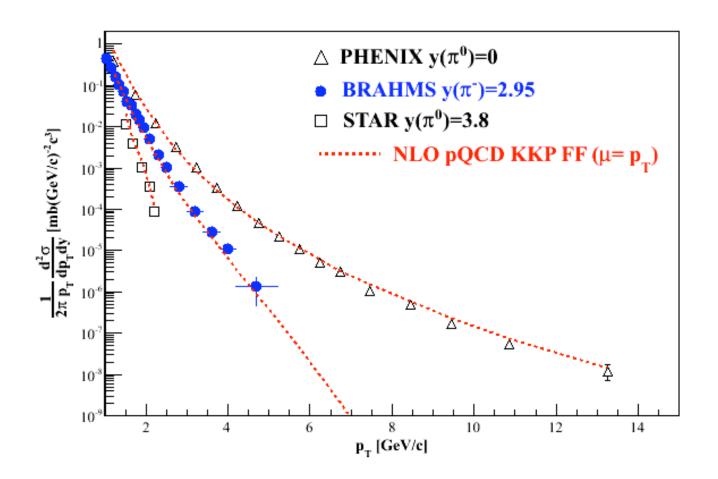
# PHENIX data on unpolarized cross section

#### BRAHMS, proton-proton at 200 GeV



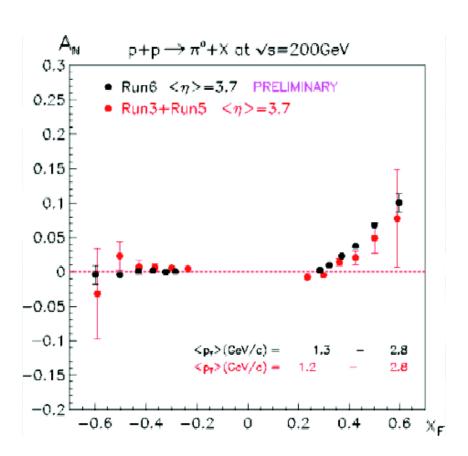
Phys. Rev. Lett. 98, 252001 (2007)

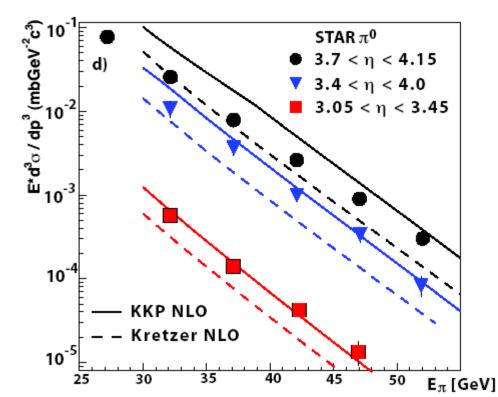
### Polarization-averaged cross sections at √s=200 GeV (talk of C. Aidala at Transversity 2008, May 2008, Ferrara)



good pQCD description of data at 200 GeV, at all rapidities, down to  $p_{\top}$  of 1-2 GeV/c

### but problems with SSAs ...



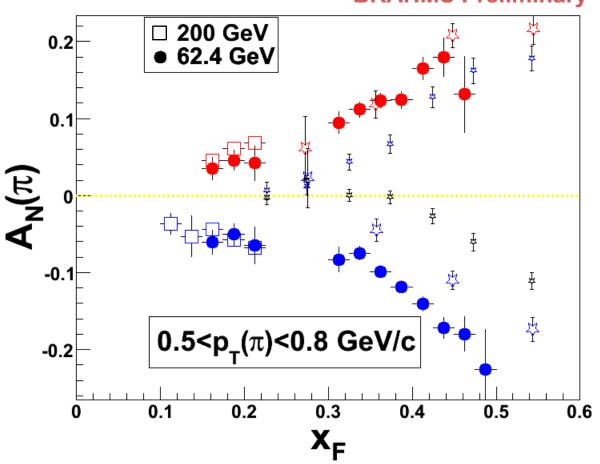


STAR-RHIC  $\sqrt{s} = 200 \text{ GeV}$  1.2 <  $p_T < 2.8$ 

#### Unifying 62.4 and 200 GeV, BRAHMS + E704

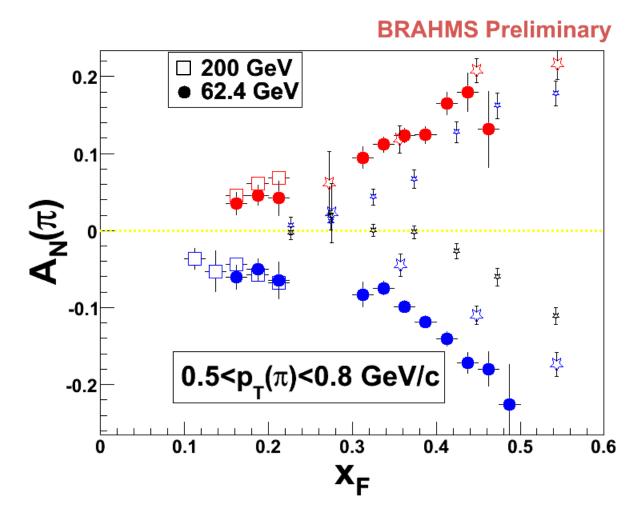
(C. Aidala talk at transversity 2008, Ferrara)





#### Unifying 62.4 and 200 GeV, BRAHMS + E704

(C. Aidala talk at transversity 2008, Ferrara)

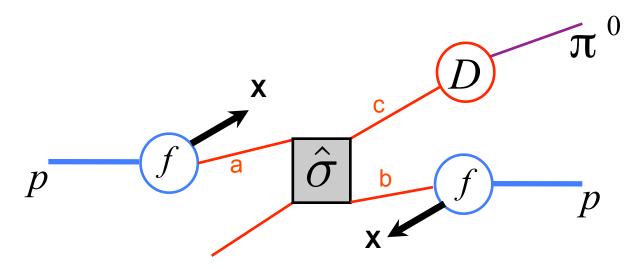


E704 data - all  $p_T$  (small stars);  $p_T>0.7$  GeV/c (large stars)

SSA in hadronic processes: intrinsic  $k_{\perp}$ , factorization?

Two main different (?) approaches

Generalization of collinear scheme (assuming factorization)



$$d\sigma = \sum_{a,b,c=q,\bar{q},g} f_{a/p}(x_a, \boldsymbol{k}_{\perp a}) \otimes f_{b/p}(x_b, \boldsymbol{k}_{\perp b}) \otimes d\hat{\sigma}^{ab \to cd}(\boldsymbol{k}_{\perp a}, \boldsymbol{k}_{\perp b}) \otimes D_{\pi/c}(z, \boldsymbol{p}_{\perp \pi})$$

first proposed by Field-Feynman

#### Possible sources of SSA, simple approach (one $k_{\perp}$ at a time)

$$d\sigma^{\uparrow} - d\sigma^{\uparrow} = \sum_{a,b,c} \left\{ \Delta^{N} f_{a/p^{\uparrow}}(\mathbf{k}_{\perp}) \otimes f_{b/p} \otimes d\hat{\sigma}(\mathbf{k}_{\perp}) \otimes D_{\pi/c} \right.$$

$$+ \left. \left( h_{1}^{a/p} \right) \otimes f_{b/p} \otimes d\Delta \hat{\sigma}(\mathbf{k}_{\perp}) \otimes \Delta^{N} D_{\pi/c^{\uparrow}}(\mathbf{k}_{\perp}) \right.$$

$$+ \left. \left( h_{1}^{a/p} \right) \otimes \Delta^{N} f_{b^{\uparrow}/p}(\mathbf{k}_{\perp}) \otimes d\Delta' \hat{\sigma}(\mathbf{k}_{\perp}) \otimes D_{\pi/c} \right\}$$

- Sivers effect

(2) transversity 

 Collins

 partially suppressed

 by phases

#### General formalism with helicity amplitudes

$$\mathrm{d}\sigma^{(A,S_A)+(B,S_B)\to C+X} = \sum \rho_{\lambda_a,\lambda_a'}^{a/A,S_A} \, \hat{f}_{a/A,S_A}(x_a,\boldsymbol{k}_{\perp a}) \otimes \rho_{\lambda_b,\lambda_b'}^{b/B,S_B} \, \hat{f}_{b/B,S_B}(x_b,\boldsymbol{k}_{\perp b})$$

$$\otimes \quad \hat{M}_{\lambda_c,\lambda_d;\lambda_a,\lambda_b} \, \hat{M}^*_{\lambda_c',\lambda_d;\lambda_a',\lambda_b'}(\boldsymbol{k}_{\perp a},\boldsymbol{k}_{\perp b}) \, \hat{D}^{\lambda_C,\lambda_C}_{\lambda_c,\lambda_c'}(z,\boldsymbol{k}_{\perp C})$$

$$\text{non planar process,}$$

$$\text{plenty of phases}$$

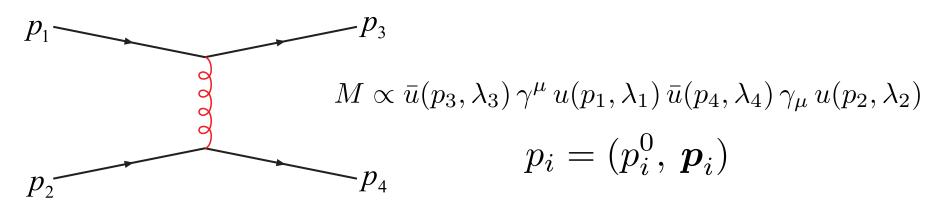
#### main (maybe) contribution to SSA from Sivers effect

$$d\Delta \sigma^{p,S+p\to\pi+X} = \sum_{q} \Delta^{N} f_{q/p^{\uparrow}}(x_{a}, \boldsymbol{k}_{\perp a}) \otimes f_{b/p}(x_{b}, \boldsymbol{k}_{\perp b})$$

$$\otimes d\hat{\sigma}^{ab\to cd}(\boldsymbol{k}_{\perp a}, \boldsymbol{k}_{\perp b}) \otimes D_{\pi/c}(z, \boldsymbol{p}_{\perp \pi})$$

M.A., M. Boglione, U. D'Alesio, E. Leader, S. Melis, F. Murgia, PR **D71**, 014002 (2005), PR **D73**, 014020 (2006)

#### Computation of helicity amplitudes



#### Dirac-Pauli helicity spinors

$$u(p_i, \lambda_i) = \sqrt{p_i^0} \begin{pmatrix} 1 \\ \lambda_i \end{pmatrix} \chi_{\lambda_i}(\hat{\boldsymbol{p}}_i) \qquad \hat{\boldsymbol{p}}_i = (\sin \theta_i \cos \phi_i, \sin \theta_i \sin \phi_i, \cos \theta_i)$$

$$\chi_+(\hat{\boldsymbol{p}}_i) = \begin{pmatrix} \cos(\theta_i/2) e^{-i\Phi_i/2} \\ \sin(\theta_i/2) e^{i\Phi_i/2} \end{pmatrix} \qquad \chi_-(\hat{\boldsymbol{p}}_i) = \begin{pmatrix} -\sin(\theta_i/2) e^{-i\Phi_i/2} \\ \cos(\theta_i/2) e^{i\Phi_i/2} \end{pmatrix}$$

if scattering is not planar all phases are different and remain in the amplitudes; they suppress the results when integrating over  $\mathbf{k}_{\perp}$ 

$$\begin{split} \frac{E_C\,d\sigma^{(A,S_A)+(B,S_B)\to C+X}}{d^3\boldsymbol{p}_C} = & \sum_{a,b,c,d,\{\lambda\}} \quad \int \frac{dx_a\,dx_b\,dz}{16\pi^2x_ax_bz^2s}\,d^2\boldsymbol{k}_{\perp a}\,d^2\boldsymbol{k}_{\perp b}\,d^3\boldsymbol{k}_{\perp C}\,\delta(\boldsymbol{k}_{\perp C}\cdot\hat{\boldsymbol{p}}_c)\,J(\boldsymbol{k}_{\perp C}) \\ & \times \; \rho^{a/A,S_A}_{\lambda_a,\lambda_a'}\,\hat{f}_{a/A,S_A}(x_a,\boldsymbol{k}_{\perp a})\;\rho^{b/B,S_B}_{\lambda_b,\lambda_b'}\,\hat{f}_{b/B,S_B}(x_b,\boldsymbol{k}_{\perp b}) \\ & \times \; \hat{M}_{\lambda_c,\lambda_d;\lambda_a,\lambda_b}\,\hat{M}^*_{\lambda_c',\lambda_d;\lambda_a',\lambda_b'}\,\delta(\hat{s}+\hat{t}+\hat{u})\;\hat{D}^{\lambda_C,\lambda_C}_{\lambda_c,\lambda_c'}(z,\boldsymbol{k}_{\perp C}) \end{split}$$

$$\rho_{\lambda_{a},\lambda_{a}'}^{a/A,S_{A}} = \begin{pmatrix} \rho_{++}^{a} & \rho_{+-}^{a} \\ \rho_{-+}^{a} & \rho_{--}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} & 1 - P_{z}^{a} \end{pmatrix}_{A,S_{A}} = \frac{1}{2} \begin{pmatrix} 1 + P_{z}^{a} & P_{x}^{a} - iP_{y}^{a} \\ P_{x}^{a} + iP_{y}^{a} &$$

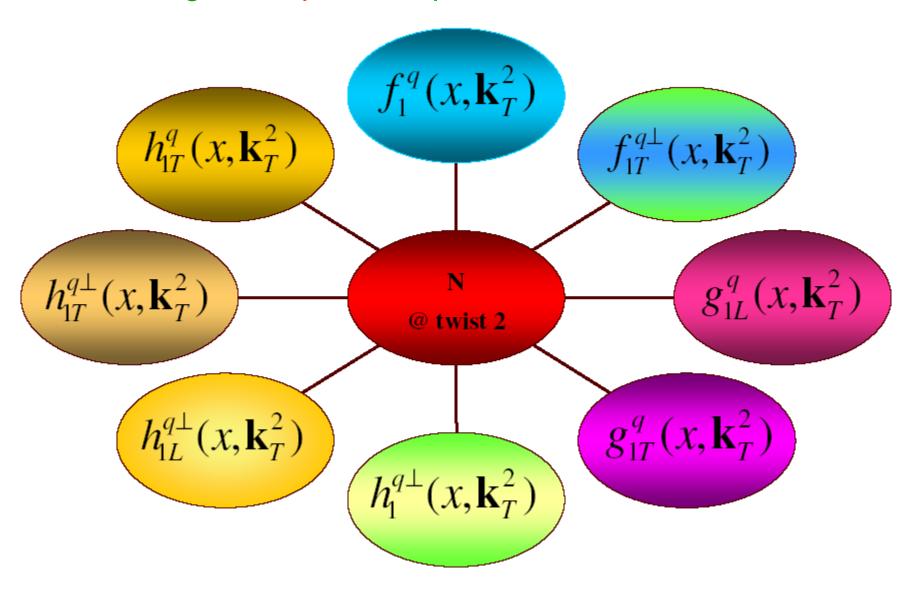
$$(P_{j}^{a} \hat{f}_{a/A,S_{Y}}) = \Delta \hat{f}_{s_{j}/S_{Y}}^{a} = \hat{f}_{s_{j}/\uparrow}^{a} - \hat{f}_{-s_{j}/\uparrow}^{a} \equiv \Delta \hat{f}_{s_{j}/\uparrow}^{a} (x_{a}, \mathbf{k}_{\perp a})$$

$$(P_{j}^{a} \hat{f}_{a/A,S_{Z}}) = \Delta \hat{f}_{s_{j}/S_{Z}}^{a} = \hat{f}_{s_{j}/+}^{a} - \hat{f}_{-s_{j}/+}^{a} \equiv \Delta \hat{f}_{s_{j}/+}^{a} (x_{a}, \mathbf{k}_{\perp a})$$

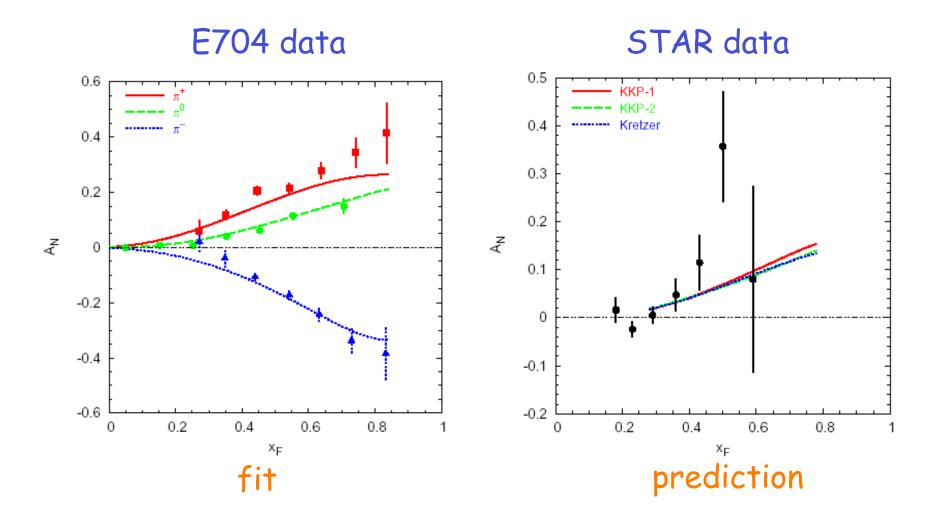
$$(\hat{f}_{a/A,S_{Y}}) = \hat{f}_{a/A}(x_{a}, k_{\perp a}) + \frac{1}{2} \Delta \hat{f}_{a/S_{Y}}(x_{a}, \mathbf{k}_{\perp a})$$

$$\hat{f}_{a/A,S_{T}} - \hat{f}_{a/A,-S_{T}} = \Delta \hat{f}_{a/S_{T}}(x_{a}, \mathbf{k}_{\perp a}) = -2 \frac{k_{\perp a}}{M} \sin(\phi_{S_{A}} - \phi_{a}) f_{1T}^{\perp}(x_{a}, k_{\perp a}) 
P_{x}^{a} \hat{f}_{a/A,S_{L}} = \Delta \hat{f}_{s_{x}/+}(x_{a}, \mathbf{k}_{\perp a}) = \frac{k_{\perp a}}{M} h_{1L}^{\perp}(x_{a}, k_{\perp a}) 
P_{y}^{a} \hat{f}_{a/A,S_{L}} = P_{y}^{a} \hat{f}_{a/A} = \Delta \hat{f}_{s_{y}/A}(x_{a}, \mathbf{k}_{\perp a}) = -\frac{k_{\perp a}}{M} h_{1}^{\perp}(x_{a}, k_{\perp a}) 
P_{z}^{a} \hat{f}_{a/A,S_{L}} = \Delta \hat{f}_{s_{z}/+}(x_{a}, \mathbf{k}_{\perp a}) = g_{1L}(x_{a}, k_{\perp a}) 
P_{z}^{a} \hat{f}_{a/A,S_{T}} = \Delta \hat{f}_{s_{z}/S_{T}}(x_{a}, \mathbf{k}_{\perp a}) = \frac{k_{\perp a}}{M} \cos(\phi_{S_{A}} - \phi_{a}) g_{1T}^{\perp}(x_{a}, k_{\perp a}) 
P_{x}^{a} \hat{f}_{a/A,S_{T}} = \Delta \hat{f}_{s_{x}/S_{T}}(x_{a}, \mathbf{k}_{\perp a}) 
= \left[ h_{1T}(x_{a}, k_{\perp a}) + \frac{k_{\perp a}^{2}}{M^{2}} h_{1T}^{\perp}(x_{a}, k_{\perp a}) \right] \cos(\phi_{S_{A}} - \phi_{a}) 
P_{y}^{a} \hat{f}_{a/A,S_{T}} = \Delta \hat{f}_{s_{y}/S_{T}}(x_{a}, \mathbf{k}_{\perp a}) 
= -\frac{k_{\perp a}}{M} h_{1}^{\perp}(x_{a}, k_{\perp a}) + h_{1T}(x_{a}, k_{\perp a}) \sin(\phi_{S_{A}} - \phi_{a})$$

#### 8 leading-twist spin-k dependent distribution functions



#### U. D'Alesio, F. Murgia



#### Higher-twist partonic correlations

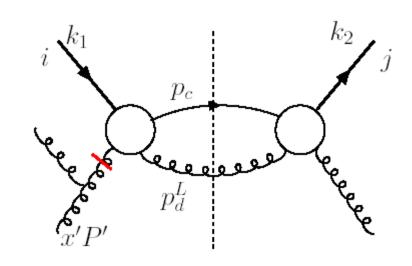
(Efremov, Teryaev; Qiu, Sterman; Kouvaris, Vogelsang, Yuan)

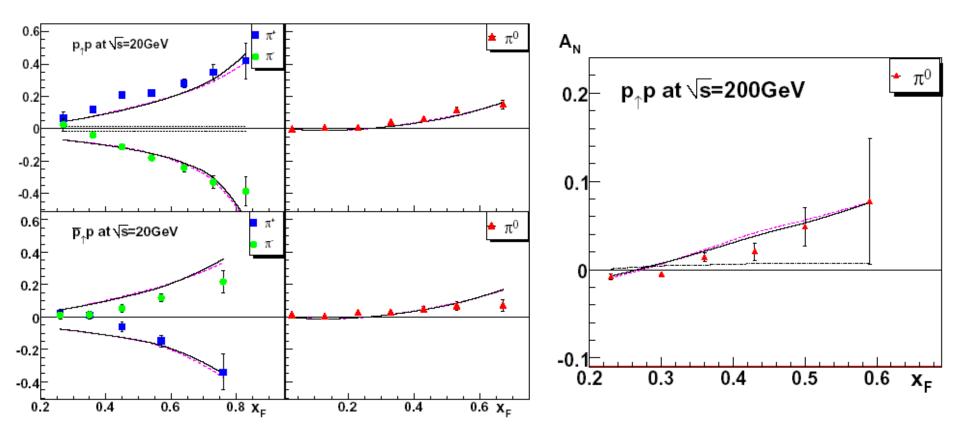
#### contribution to SSA $(A^{\uparrow}B \rightarrow h X)$

$$\mathrm{d}\Delta\sigma\propto\sum_{a,b,c}\underbrace{T_a(k_1,k_2,S_\perp)}\otimes f_{b/B}(x_b)\otimes \underbrace{H^{ab o c}(k_1,k_2)}\otimes D_{h/c}(z)$$
 twist-3 functions hard interactions

"collinear expansion" at order  $k_{i\perp}$ 

$$T_a = N_a x^{\alpha_a} (1 - x)^{\beta_a} f_{a/A}(x)$$

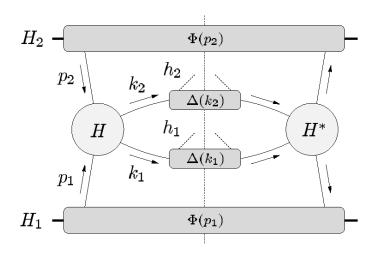




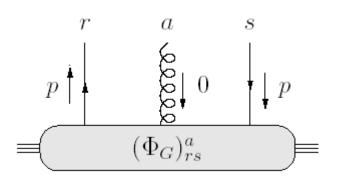
fits of E704 and STAR data Kouvaris, Qiu, Vogelsang, Yuan

#### Gluonic pole cross sections and SSA in $H_1H_2 \rightarrow h_1h_2X$

Bacchetta, Bomhof, Mulders, Pijlman; Vogelsang, Yuan; Teryaev



#### factorization?



#### Sivers contribution to SSA $(T_a \propto f_{1T}^{\perp (1)})$

$$d\Delta\sigma \propto \sum_{a,b,c} f_{1T}^{\perp(1)}(x_1) \otimes f_{b/H_2}(x_2) \otimes d\hat{\sigma}_{[a]b \to cd} \otimes D_{h_1/c}(z_1) D_{h_2/d}(z_2)$$

#### gluonic pole cross sections take into account gauge links

$$\mathrm{d}\hat{\sigma}_{[a]b\to cd} = \sum_{D} C_G^{[D]} \; \mathrm{d}\hat{\sigma}_{ab\to cd}^{D} \qquad C_G^{[D]} \; \underset{\mathrm{link}\; \mathit{Colour}\; \mathrm{factors}}{\mathrm{biagram}} \; \mathrm{dependent}\; \mathit{Gauge}$$

(breaking of factorization?)

#### Gluonic pole cross sections and SSA in $H_1H_2 ightarrow h_1h_2X$

$$\frac{d\hat{\sigma}_{[q]q \to qq}}{d\hat{t}} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{3}{2} + \frac{3}$$

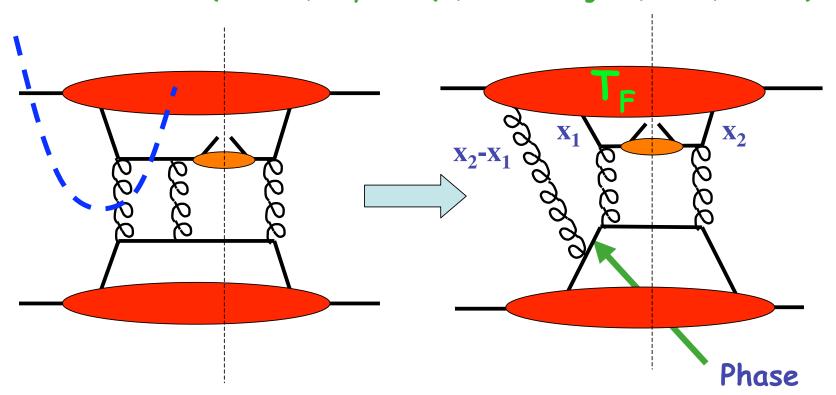
#### to be compared with the usual cross section

$$\frac{d\hat{\sigma}_{qq \to qq}}{d\hat{t}} = \frac{1}{2} + \frac{1}{2$$

$$d\hat{\sigma}_{[\ell]q\to\ell q} = d\hat{\sigma}_{\ell q\to\ell q} \qquad d\hat{\sigma}_{[q]\bar{q}\to\ell^+\ell^-} = -d\hat{\sigma}_{q\bar{q}\to\ell^+\ell^-}$$

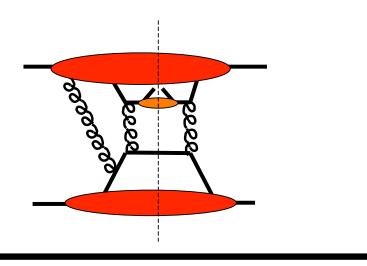
#### From W. Vogelsang talk at Beijing 2008

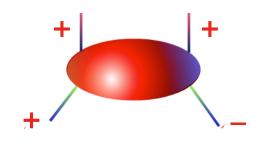
power-suppressed effects in QCD much richer than
 mass terms (Efremov, Teryaev; Qiu, Sterman; Eguchi, Koike, Tanaka)



Collinear factorization in terms of "quark-gluon correlation":

$$T_F(x,x) = \int rac{dy_1^-}{4\pi} e^{ixP^+y_1^-} \langle P, \vec{s}_T | \bar{\psi}_a(0) \gamma^+ \left[ \int dy_2^- \epsilon^{s_T \sigma n \bar{n}} F_{\sigma}^+(y_2^-) 
ight] \psi_a(y_1^-) | P, \vec{s}_T 
angle$$





- phase in hard scattering
- hel. flip because of qgq
- factorization for pp→πX
   established
- phenomenology

Qiu, Sterman Kouvaris, Qiu, WV, Yuan

- phase in distribution fct.
   (but where exactly?)
- hel. flip because of OAM
- factorization for pp→πX
   assumed
- phenomenology

Anselmino, Boglione, D'Alesio, Leader, Melis, Murgia, ...

#### Crucial role of gauge-links in TMDs

Brodsky, Hwang, Schmidt; Collins; Belitsky, Ji, Yuan;

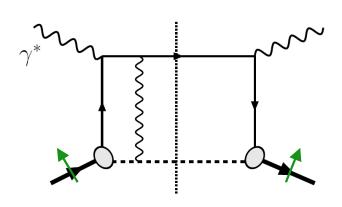
• profound implication:

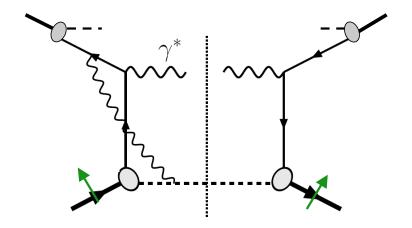
process-dependece of Sivers functions

$$f_{\mathrm{DY}}^{\mathrm{Sivers}}(x, k_{\perp}) = -f_{\mathrm{DIS}}^{\mathrm{Sivers}}(x, k_{\perp})$$

DIS: "attractive"

DY: "repulsive"

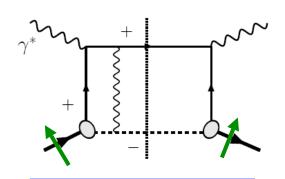




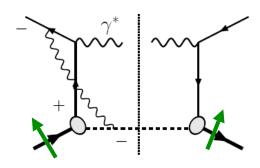
 hugely important in QCD -- tests a lot of what we know about description of hard processes

## **Non-universality** of Sivers Asymmetries: Unique Prediction of Gauge Theory!

Simple QED example:

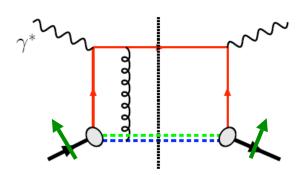


**DIS:** attractive



**Drell-Yan: repulsive** 

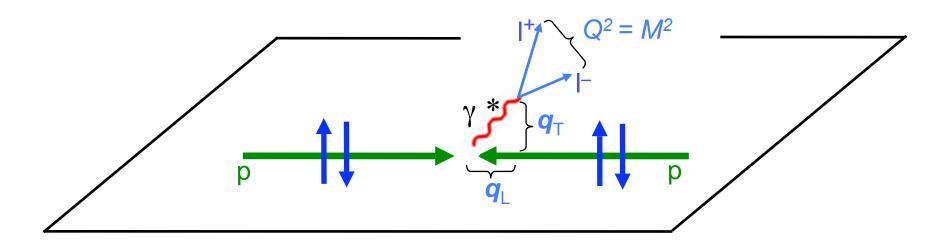
Same in QCD:



As a result:

$$Sivers|_{DIS} = -Sivers|_{DY}$$

#### TMDs and SSAs in Drell-Yan processes



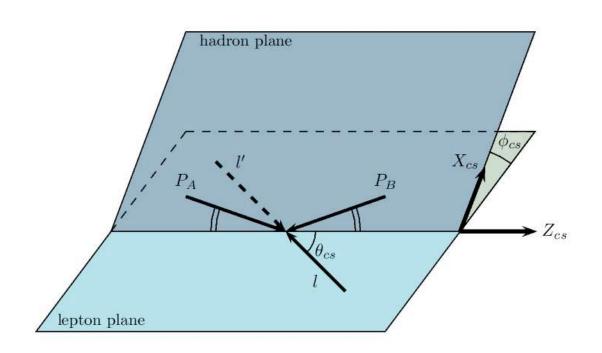
factorization holds, two scales,  $M^2$ , and  $q_T$ 

$$d\sigma^{D-Y} = \sum_{a} f_q(x_1, \boldsymbol{k}_{\perp 1}; Q^2) \otimes f_{\bar{q}}(x_2, \boldsymbol{k}_{\perp 2}; Q^2) d\hat{\sigma}^{q\bar{q} \to \ell^+ \ell^-}$$

3 planes: plane  $\perp$  to polarization vectors,  $p - \gamma$  \* plane,  $l^+ - l^-$  plane no fragmentation process

#### Unpolarized cross section already very interesting

$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega} = \frac{3}{4\pi} \frac{1}{\lambda + 3} \left( 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right)$$



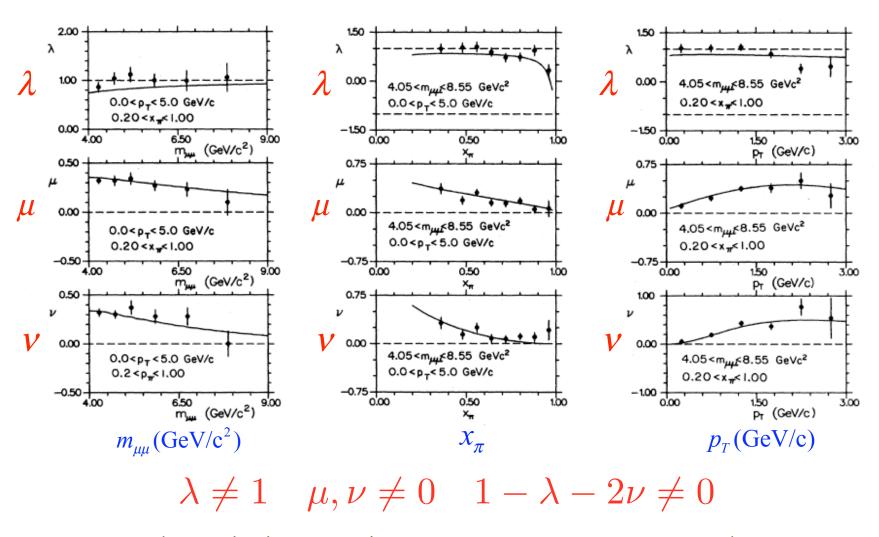
Collins-Soper frame

naive collinear parton model:  $\lambda=1$   $\mu=
u=0$ 

#### Decay angular distributions in pion-induced Drell-Yan

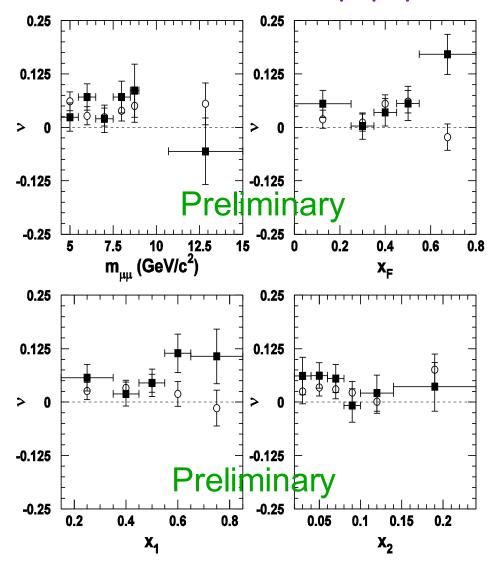
E615 Data 252 GeV  $\pi^{-}$  + W

Phys. Rev. D 39 (1989) 92



(Jen-Chieh Peng talk at transversity 2008, Ferrara)

#### Angular Distribution in E866 p+p/p+d Drell-Yan



PRL 99 (2007) 082301

### TMDs help: for example, the cos $2\phi$ term can be originated by the Boer-Mulders effect

$$d\sigma \propto d\sigma^{0} + \sum_{q} h_{1q}^{\perp}(x_{1}, k_{\perp}) \otimes h_{1\bar{q}}^{\perp}(x_{2}, k_{\perp}) \otimes \underbrace{(d\hat{\sigma}^{\uparrow\uparrow} - d\hat{\sigma}^{\uparrow\downarrow})}_{\sin^{2}\theta \cos 2\phi}$$

Polarized D-Y processes with intrinsic  $k_{\perp}$  have a rich structure, similar to SIDIS

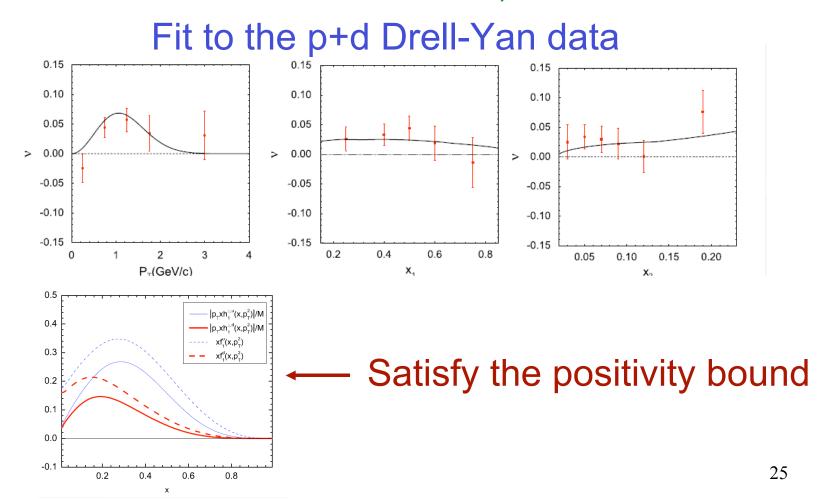
SSA in D-Y has a contribution from the coupling of the transversity distribution to B-M function

$$d\sigma^{\uparrow} - d\sigma^{\downarrow} \propto \sum_{q} h_{1q}(x_1) \otimes h_{1\bar{q}}^{\downarrow}(x_2, k_{\perp}) \otimes \underbrace{(d\hat{\sigma}^{\uparrow\uparrow} - d\hat{\sigma}^{\uparrow\downarrow})}_{\cos 2\phi}$$

B-M 
$$f_{q,\mathbf{s}_q/p}(x,\mathbf{k}_{\perp}) = \frac{1}{2} f_{q/p}(x,k_{\perp}) - \frac{k_{\perp}}{2M} h_{1q}^{\perp}(x,k_{\perp}) \mathbf{s}_q \cdot (\hat{\boldsymbol{p}} \times \hat{\boldsymbol{k}}_{\perp})$$

## Extraction of Boer-Mulders functions from p+d Drell-Yan

(B. Zhang, Z. Lu, B-Q. Ma and I. Schmidt, arXiv:0803.1692)



#### Sivers effect in D-Y processes

By looking at the  $d^4\sigma/d^4q$  cross section one can single out the Sivers effect in D-Y processes

$$d\sigma^{\uparrow} - d\sigma^{\downarrow} \propto \sum_{q} \Delta^{N} f_{q/p}(x_1, k_{\perp}) \otimes f_{\bar{q}/p}(x_2) \otimes d\hat{\sigma}$$

$$A_{N} = \frac{\mathrm{d}\sigma^{\uparrow} - \mathrm{d}\sigma^{\downarrow}}{\mathrm{d}\sigma^{\uparrow} + \mathrm{d}\sigma^{\downarrow}}$$

$$\sum_{q} e_{q}^{2} \int d^{2}\mathbf{k}_{\perp q} d^{2}\mathbf{k}_{\perp \bar{q}} \delta^{2}(\mathbf{k}_{\perp q} + \mathbf{k}_{\perp \bar{q}} - \mathbf{q}_{T}) \underbrace{\Delta^{N} f_{q/p^{\uparrow}}(x_{q}, \mathbf{k}_{\perp})} f_{\bar{q}/p^{\uparrow}}(x_{\bar{q}}, \mathbf{k}_{\perp \bar{q}})$$

$$2 \sum_{q} e_{q}^{2} \int d^{2}\mathbf{k}_{\perp q} d^{2}\mathbf{k}_{\perp \bar{q}} \delta^{2}(\mathbf{k}_{\perp q} + \mathbf{k}_{\perp \bar{q}} - \mathbf{q}_{T}) f_{q/p^{\uparrow}}(x_{q}, \mathbf{k}_{\perp}) f_{\bar{q}/p^{\uparrow}}(x_{\bar{q}}, \mathbf{k}_{\perp \bar{q}})$$

$$q = u, \bar{u}, d, \bar{d}, s, \bar{s}$$

$$A_N^{\sin(\phi_S - \phi_\gamma)} \equiv \frac{2\int_0^{2\pi} \! \mathrm{d}\phi_\gamma \left[\mathrm{d}\sigma^\uparrow - \mathrm{d}\sigma^\downarrow\right] \sin(\phi_S - \phi_\gamma)}{\int_0^{2\pi} \! \mathrm{d}\phi_\gamma \left[\mathrm{d}\sigma^\uparrow + \mathrm{d}\sigma^\downarrow\right]} \quad \text{(p-p c.m. frame)}$$

#### Predictions for $A_N$ at RHIC (S. Melis)

#### Sivers functions as extracted by

M.A., M. Boglione, U. D'Alesio, A. Kotzinian, S. Melis, F. Murgia, A. Prokudin and C. Türk from SIDIS data, with opposite sign

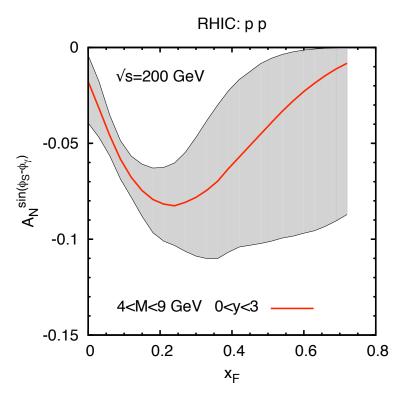


Figure 9: The single spin asymmetries  $A_N^{\sin(\phi_S - \phi_\gamma)}$  for the Drell-Yan process  $p^{\uparrow}p \to \mu^{+}\mu^{-} + X$  at RHIC, as function of  $x_F = x_a - x_b$ , averaged over the invariant mass range 4 < M < 9, rapidity 0 < y < 3 and transverse momentum  $0 < q_T < 1 \text{ GeV}/c$ , for  $\sqrt{s} = 200 \text{ GeV}$ .

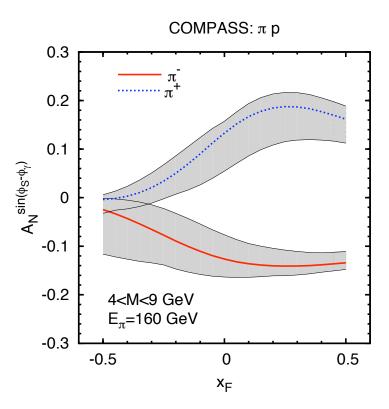


Figure 1: The single spin asymmetries  $A_N^{\sin(\phi_S-\phi_\gamma)}$  for the Drell-Yan process  $\pi p \to \mu^+ \mu^- + X$  at COMPASS, as function of  $x_F = x_a - x_b$ , averaged over the invariant mass range 4 < M < 9 and transverse momentum  $0 < q_T < 1~{\rm GeV}/c$ , for a pion beam energy of 160 GeV/c.

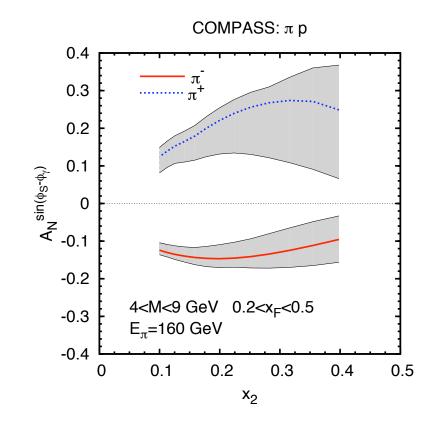


Figure 2: The single spin asymmetries  $A_N^{\sin(\phi_S - \phi_\gamma)}$  for the Drell-Yan process  $\pi p \to \mu^+ \mu^- + X$  at COMPASS, as function of  $x_b$ , averaged over the invariant mass range 4 < M < 9,  $0.2 < x_F < 0.5$  and transverse momentum  $0 < q_T < 1$  GeV/c, for a pion beam energy of 160 GeV/c. MRSS92 pion pdf

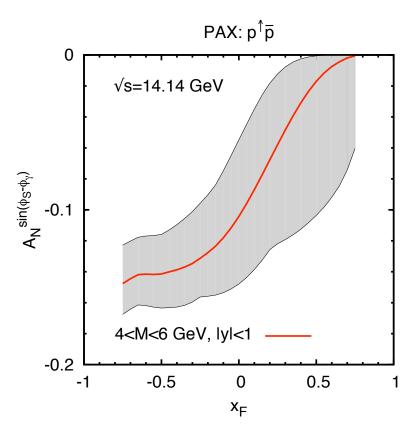
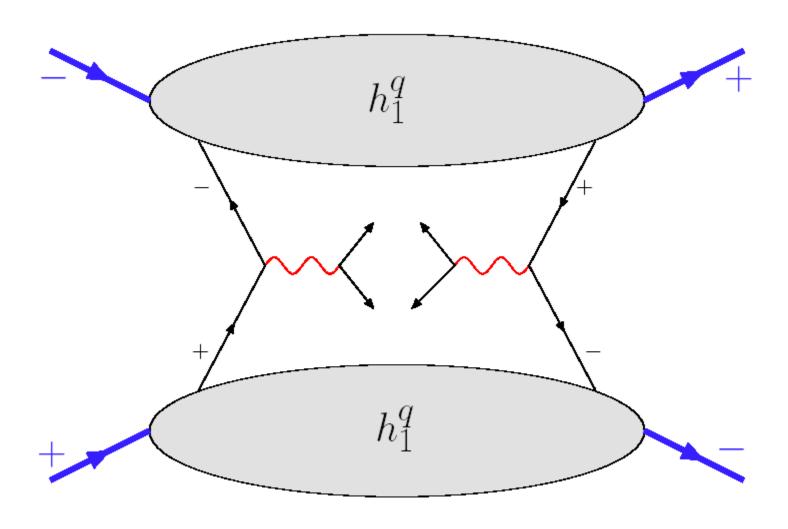


Figure 6: The single spin asymmetries  $A_N^{\sin(\phi_S-\phi_\gamma)}$  for the Drell-Yan process  $p^{\uparrow}\bar{p} \to \mu^{+}\mu^{-} + X$  at PAX, as function of  $x_F = x_a - x_b$ , averaged over the invariant mass range 4 < M < 6, rapidity |y| < 1 and transverse momentum  $0 < q_T < 1 \text{ GeV}/c$ , for  $\sqrt{s} = 14 \text{ GeV}$ .

#### Possible direct access to transversity: Drell-Yan processes

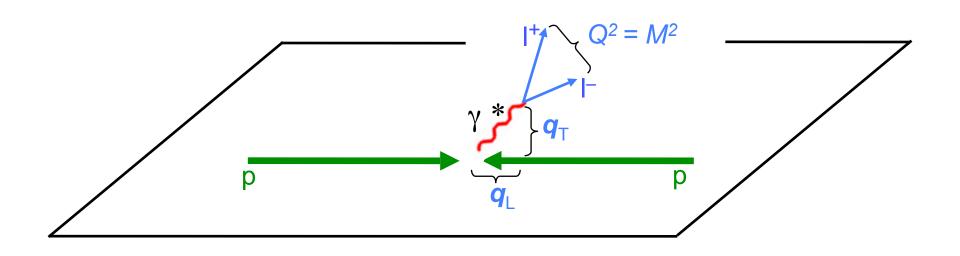
$$p p \to \ell^+ \ell^-, \ \pi p \to \ell^+ \ell^-, \ p \bar{p} \to \ell^+ \ell^-$$



#### Simple partonic cross section at collinear level

$$\frac{\mathrm{d}^2 \sigma}{\mathrm{d}M^2 \,\mathrm{d}x_F} = \frac{4\pi\alpha^2}{9M^2 s} \, \frac{1}{x_1 + x_2} \sum_q e_q^2 \left[ q(x_1, Q^2) \, \bar{q}(x_2, Q^2) + \bar{q}(x_1, Q^2) \, q(x_2, Q^2) \right]$$
$$x_F = x_1 - x_2 \qquad x_1 \, x_2 = M^2 / s \equiv \tau \qquad x_F = 2q_L / \sqrt{s}$$

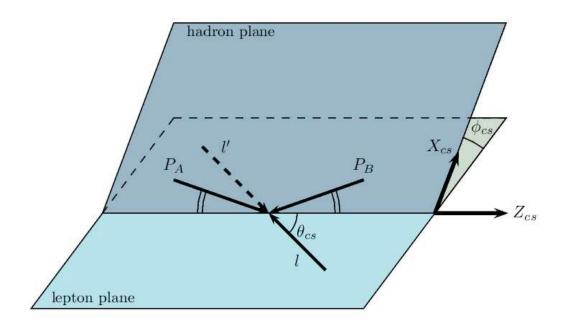
#### range of $x_1$ , $x_2$ explored depends on $\tau$



## Direct access to transversity from double transverse spin asymmetry

$$A_{_{TT}} = \frac{\mathrm{d}\sigma^{\uparrow\uparrow} - \mathrm{d}\sigma^{\uparrow\downarrow}}{\mathrm{d}\sigma^{\uparrow\uparrow} + \mathrm{d}\sigma^{\uparrow\downarrow}} = \hat{a}_{_{TT}} \frac{\sum_{q} e_{q}^{2} \left[ h_{1q}(x_{1}) \, h_{1\bar{q}}(x_{2}) + h_{1\bar{q}}(x_{1}) \, h_{1q}(x_{2}) \right]}{\sum_{q} e_{q}^{2} \left[ q(x_{1}) \, \bar{q}(x_{2}) + \bar{q}(x_{1}) \, q(x_{2}) \right]}$$

$$\hat{a}_{TT} = \frac{\mathrm{d}\hat{\sigma}^{\uparrow\uparrow} - \mathrm{d}\hat{\sigma}^{\uparrow\downarrow}}{\mathrm{d}\hat{\sigma}^{\uparrow\uparrow} + \mathrm{d}\hat{\sigma}^{\uparrow\downarrow}} = \frac{\sin^2\theta}{1 + \cos^2\theta} \, \cos(2\phi)$$



RHIC energies: 
$$\sqrt{s} = 200 \, \mathrm{GeV}$$
  $M^2 \leq 100 \, \mathrm{GeV}$ 



 $au \leq 2 \cdot 10^{-3} \,$  small  $\mathbf{x_1}$  and/or  $\mathbf{x_2}$ 

 $h_{1q}(x, Q^2)$  evolution much slower than  $\Delta q(x, Q^2)$  and  $q(x, Q^2)$  at small x

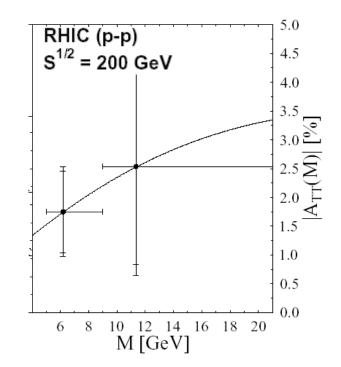


 $A_{TT}$  at RHIC is very small smaller s would help

Barone, Calarco, Drago Martin, Schäfer, Stratmann, Vogelsang

 $A_{TT}$  for Drell-Yan processes at RHIC

upgrades in luminosity expected

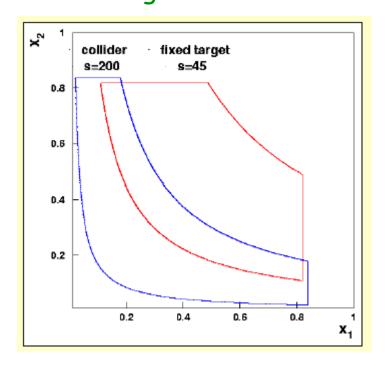


### $h_1$ from $p^{\uparrow} \bar{p}^{\uparrow} \rightarrow \ell^+ \ell^- X$ at GSI

$$A_{TT} = \frac{d\sigma^{\uparrow\uparrow} - d\sigma^{\uparrow\downarrow}}{d\sigma^{\uparrow\uparrow} + d\sigma^{\uparrow\downarrow}} = \hat{a}_{TT} \frac{\sum_{q} e_{q}^{2} \left[ h_{1q}(x_{1}) h_{1q}(x_{2}) + h_{1\bar{q}}(x_{1}) h_{1\bar{q}}(x_{2}) \right]}{\sum_{q} e_{q}^{2} \left[ q(x_{1}) q(x_{2}) + \bar{q}(x_{1}) \bar{q}(x_{2}) \right]} \simeq \hat{a}_{TT} \frac{h_{1u}(x_{1}) h_{1u}(x_{2})}{u(x_{1}) u(x_{2})}$$

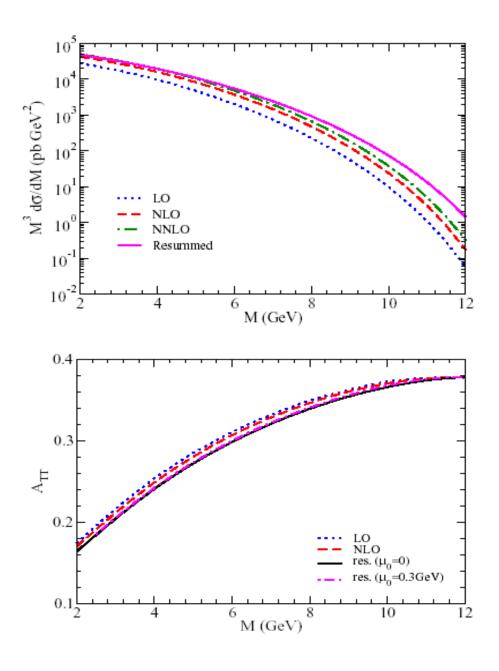
GSI energies:  $s = 30 - 210 \, {\rm GeV}^2$   $M^2 > 2 \, {\rm GeV}^2$ 

large  $x_1, x_2$ 



one measures h<sub>1</sub> in the quark valence region:  $A_{TT}$  is estimated to be large, between 0.2 and 0.4

PAX proposal: hep-ex/0505054



### results for ATT stable under QCD corrections

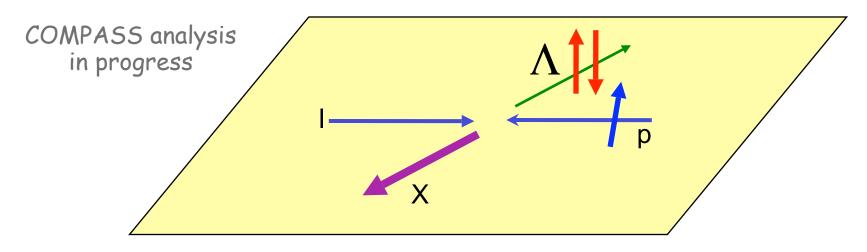
H. Shimizu, G. Sterman, W. Vogelsang and H. Yokoya

M. Guzzi, V. Barone,
A. Cafarella, C. Corianò
and P.G. Ratcliffe

#### Some alternative accesses to transversity

Inclusive  $\Lambda$  production and measure of  $\Lambda$  polarization

need to know transverse fragmentation function  $\Delta_T D = D_{q^\uparrow}^{\Lambda^\uparrow} - D_{q^\uparrow}^{\Lambda^\downarrow}$ 



the  $\Lambda$  polarization vector measured from the proton angular distribution in the  $\Lambda \to \pi p$  decay in the  $\Lambda$  helicity rest frame

$$W(\theta_p, \phi_p) = \frac{1}{4\pi} \left[ 1 + \alpha (P_z \cos \theta_p + P_x \sin \theta_p \cos \phi_p + P_y \sin \theta_p \sin \phi_p) \right]$$
$$= \frac{1}{4\pi} \left[ 1 + \mathbf{P} \cdot \hat{\mathbf{p}} \right]$$
$$\alpha = 0.642 \pm 0.013$$

### collinear configuration, no need for intrinsic $k_{\perp}$

$$P_N^{[0S_N]} = \frac{2(1-y)}{1+(1-y)^2} \, \frac{\sum_q e_q^2 \, h_{1q}(x) \, \Delta_T D_{\Lambda/q}(z)}{\sum_q e_q^2 \, q(x) \, D_{\Lambda/q}(z)}$$

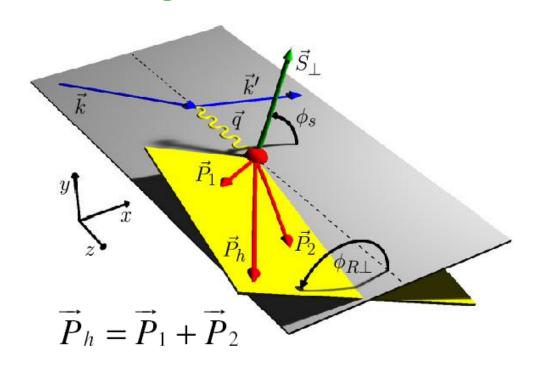
$$\Delta_T D = D_{q^{\uparrow}}^{\Lambda^{\uparrow}} - D_{q^{\uparrow}}^{\Lambda^{\downarrow}}$$

$$P_N^{[0S_N]} \simeq \frac{2(1-y)}{1+(1-y)^2} \frac{4h_{1u} + h_{1d}}{4u+d} \frac{\Delta_T D_{\Lambda/u}}{D_{\Lambda/u}}$$

similar result in  $p\,p^\uparrow o \Lambda^\uparrow\, X$ 

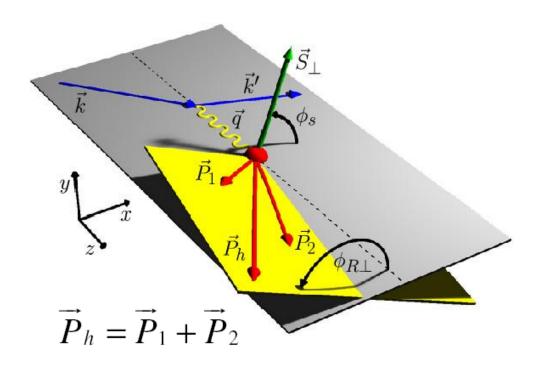
$$P_N(\Lambda) \sim \sum_{abc} f_{a/p} \otimes h_{1b} \otimes d\Delta \sigma^{ab \to c \cdots} \otimes \Delta_T D_{\Lambda/c}$$

# Two hadron production in SIDIS Di-hadron Fragmentation Function (DiFF)



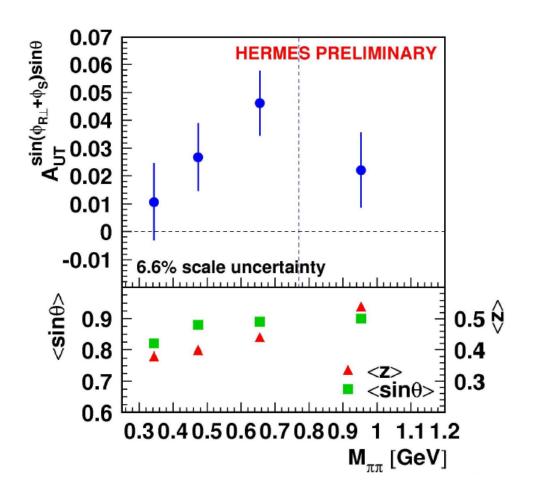
Chiral odd fragmentation function of a transversely polarized quark into two hadrons (interference between s and p wave)

# Two hadron production in SIDIS Di-hadron Fragmentation Function (DiFF)



Chiral odd fragmentation function of a transversely polarized quark into two hadrons (interference between s and p wave)

Bacchetta, Boer, Jaffe, Jakob, Radici ...



$$A_{UT} = \frac{\mathrm{d}\sigma^{\uparrow} - \mathrm{d}\sigma^{\downarrow}}{\mathrm{d}\sigma^{\uparrow} + \mathrm{d}\sigma^{\downarrow}} \propto \sin(\Phi_{R\perp} + \Phi_{S}) \frac{\sum_{q} e_{q}^{2} h_{1q} H_{1}^{DiFF}}{\sum_{q} e_{q}^{2} f_{1q} D}$$

## Not all spin problems have been solved, but enormous progress has been made

The spin-orbiting structure of quarks in nucleons begins to emerge

Theory. Unintegrated PDF and FF play a crucial role; their Q<sup>2</sup> evolution is needed. Factorization and universality issues must be clarified, ...

Experiment. New data from COMPASS (proton target), JLab, RHIC, and GSI. D-Y processes very promising ...